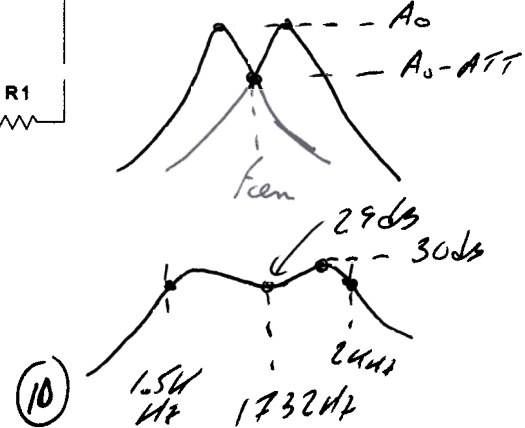
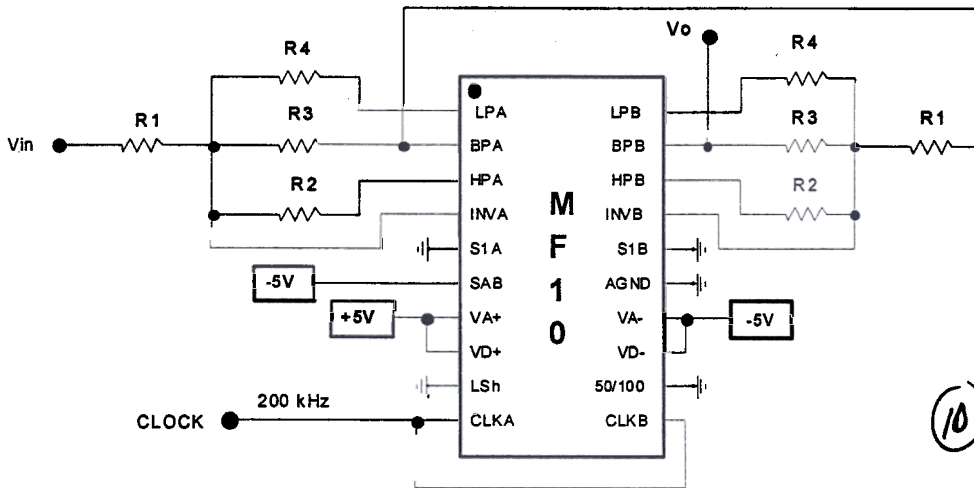


NAME: SOLUTIONS

No.1 (50 pts) $F_n = \frac{F_{clk}}{100} \times \sqrt{\frac{R_2}{R_4}}$ $Q = \frac{R_3}{\sqrt{R_2 R_4}}$ $A_{HP} = -\frac{R_3}{R_1} = -38.174$

$ATT(dB) = 10 \times \text{LOG} \left(1 + Q^2 \left(\frac{F_n}{F} - \frac{F}{F_n} \right)^2 \right) = 10 \cdot \text{LOG} \left(1 + 25.075^2 \left(\frac{1995.3}{1732} - \frac{1732}{1995.3} \right)^2 \right) = 17.134 \text{ dB}$



$\omega_{cut} = 3.4641$

Design a band-pass filter that meets the following specifications:

$A_0 = (29 + 2 \cdot 17.134) / 2 = 31.63 \text{ dB}$

- Pass-band gain of 30 dB
- Cutoff frequencies of 1500 Hz and 2000 Hz
- Chebyshev response with 1 dB ripple.
- Normalised low-pass poles $0.99323 \angle \pm 98.076^\circ$

$S_{1,2} = 3.99062 \angle \pm 91.14257^\circ$
 $S_{3,4} = 3.00705 \angle \pm 91.14257^\circ$
 $0.52858 \angle \pm 129.591^\circ$

$S_{1,2} = 12536.9 \angle \pm 91.14257^\circ$

$S_{3,4} = 9946.9 \angle \pm 91.14257^\circ$

$Q_1 = 25.075$ $F_{n1} = 1995.34 \text{ Hz}$ $A_0 = 38.174$ (31.634 dB)

$F_{n2} = 1503.54 \text{ Hz}$ $Q_2 = 25.075$ $A_0 = 38.174$

$\frac{R_2}{R_4} = \left(\frac{100 F_{n1}}{F_{cut1}} \right)^2 = 0.9983$

$\frac{R_2}{R_4} = 0.565125$

$R_3 = 25.075 \sqrt{R_2 R_4}$

$R_3 = 25.075 \sqrt{R_2 R_4}$

$R_1 = R_3 / 38.17$

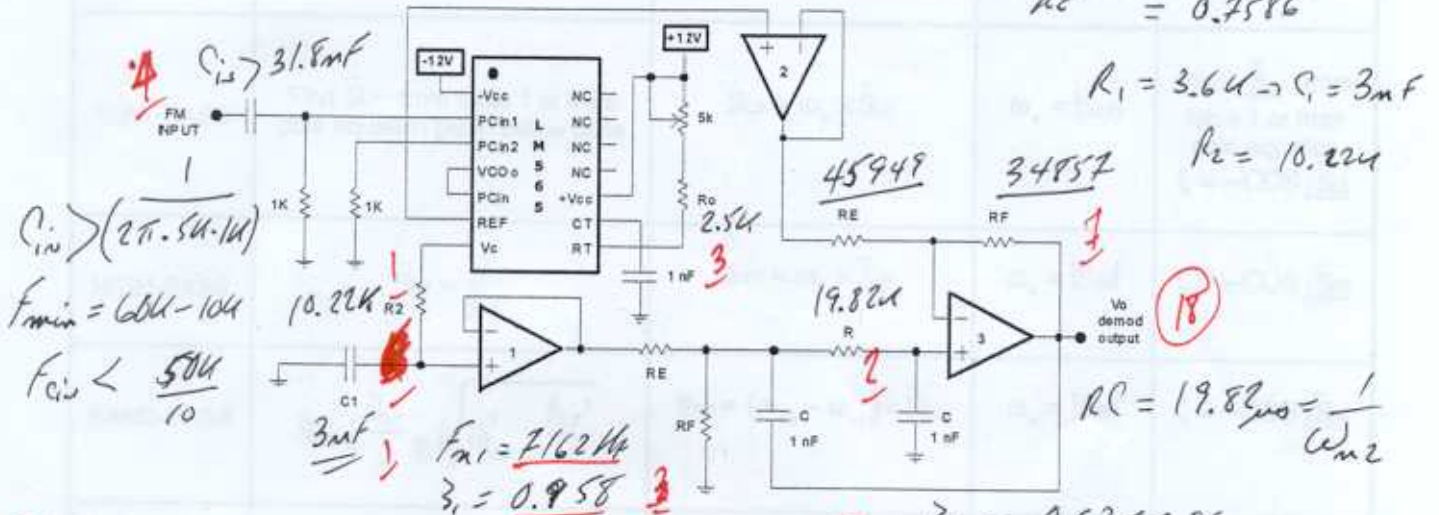
$R_1 = R_3 / 38.17$

(24)

No.2 (50 pts) $F_{cen} \approx 0.3 / ((R_o + P_o)C_o)$ $K_d \approx 0.68 \frac{V}{rad}$ $K_o = \frac{\Delta\omega_{in}}{\Delta V_{C(Thev)}} \approx \frac{49.4 F_{cen}}{\Delta V_{CC}} = 123.54$

$R_1 = 3.6K$ $\tau_1 + \tau_2 = \frac{K_o K_d}{\omega_n^2} = 41.47 \mu s$ $\tau_2 = \frac{2\zeta}{\omega_n} - \frac{1}{K_o K_d} = 30.67 \mu s$ $\tau_1 = 10.8 \mu s$

Sallen-Key stage: $A_o = \frac{R_F}{R_E}$ $\omega_n = \frac{1}{RC}$ if $R = R_E || R_F$ $\zeta = 1 - \frac{R_F}{2R_E} \Rightarrow R_E = 2(1 - \zeta)$
 $R_E = 0.7586$



A(30) Design the above PLL to meet the following specs:

FM input: $F_{car} = 60 \text{ kHz}$ $\Delta F = 0 \text{ to } 10 \text{ kHz}$ $F_{mod} = 0 \text{ to } 2.5 \text{ kHz}$

PLL demodulator response: 4th order low-pass Bessel with 5 kHz bandwidth.

Normalised poles: $1.43241 \angle \pm 163.332^\circ$ $1.60594 \angle \pm 128.367^\circ$
 $45800 \angle \pm \phi_1$ $50452 \angle \pm \phi_2$

B(10) Calculate the demodulated signal amplitude and explain the function of the Sallen-Key stage.

$\Delta V_c = 2\pi \cdot 10k / 123.54 = 0.50884\mu$ $\Delta V_{demod} = 0.3864\mu$

C(10) Determine the phase error signal when ΔF of carrier is maximum and F_{mod} is 2.5 kHz

Sketch signal showing max, min and average value of phase error.

- Eliminate DC
- Component
- Attenuate HF ripple

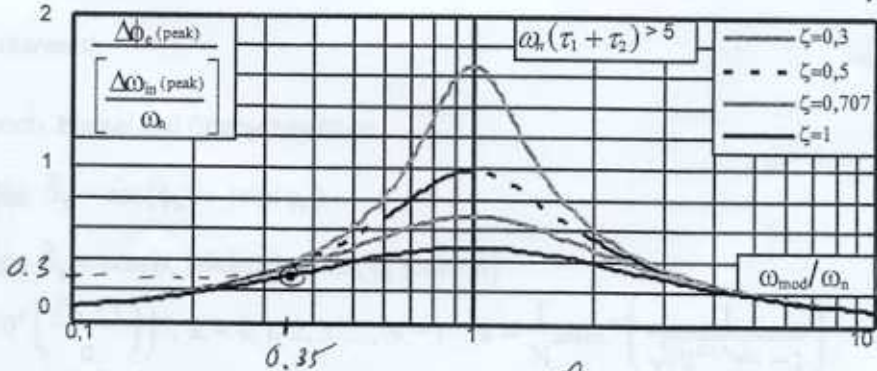
Normalised phase error for FM sinusoidal modulation

$\omega_n(\tau_1 + \tau_2) = 1.866$

Use the following expression

$\omega_n(\tau_1 + \tau_2) = K_o K_d / \omega_n$ to find out if the graph shown beside applies.

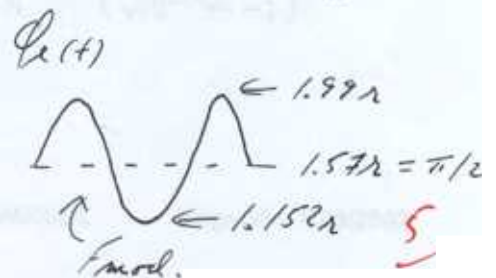
Graph does not apply here!
 let's assume it does not



$\frac{F_{mod}}{F_{m1}} = 0 \rightarrow \frac{2.5k}{7162}$

$\frac{F_{mod}}{F_{m1}} = 0 \rightarrow 0.35$

$\Delta\phi_e(\phi) = 0.3 \times 10k / 7162 = 0.4198$



10